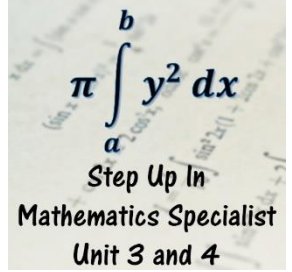


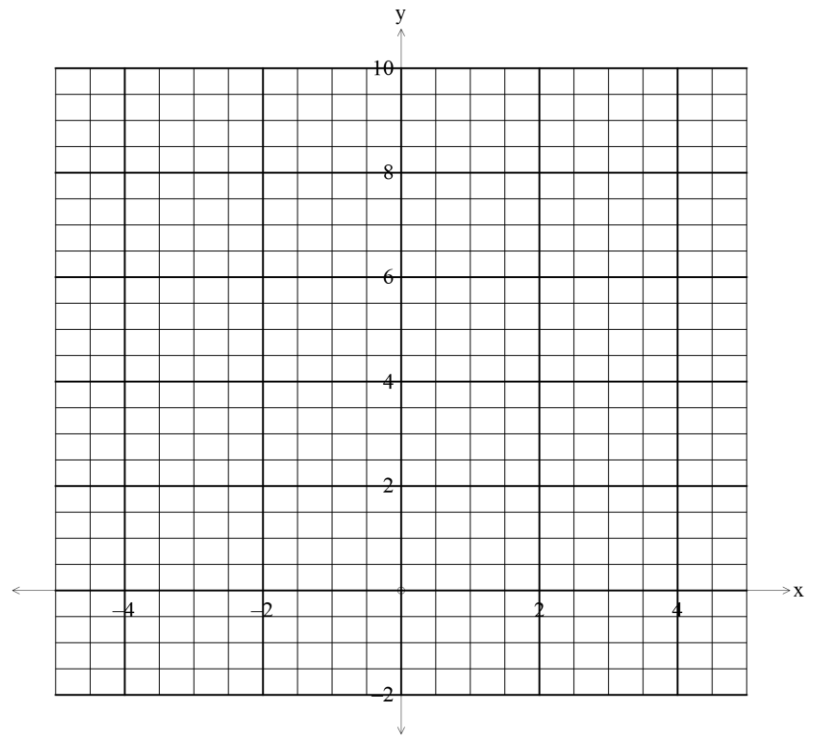
# 2.3 Absolute Value Functions

## Problems Worksheet

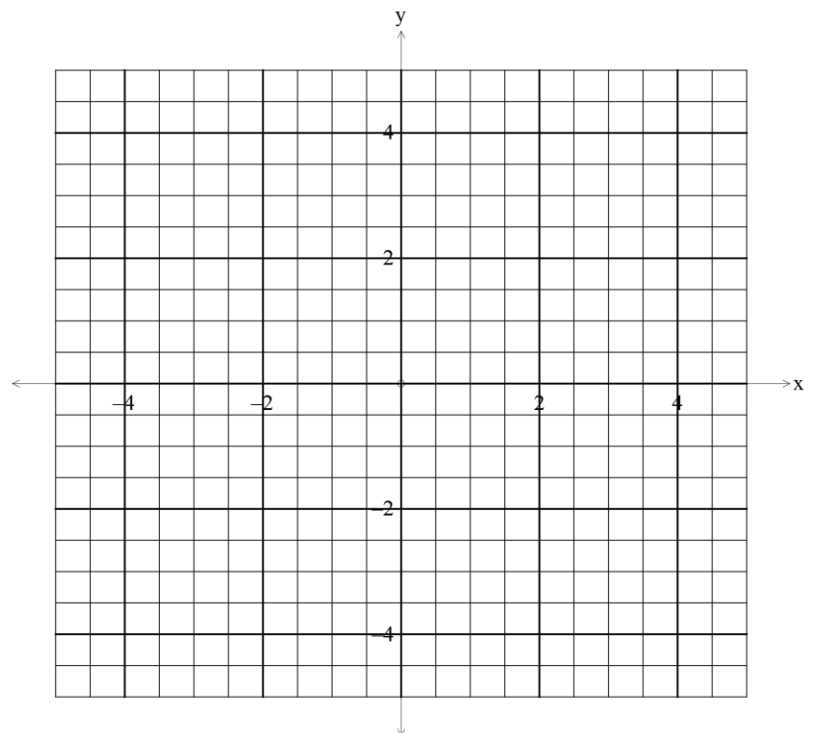


1. For each of the following functions, first write them as piecewise-defined functions, and then sketch them.

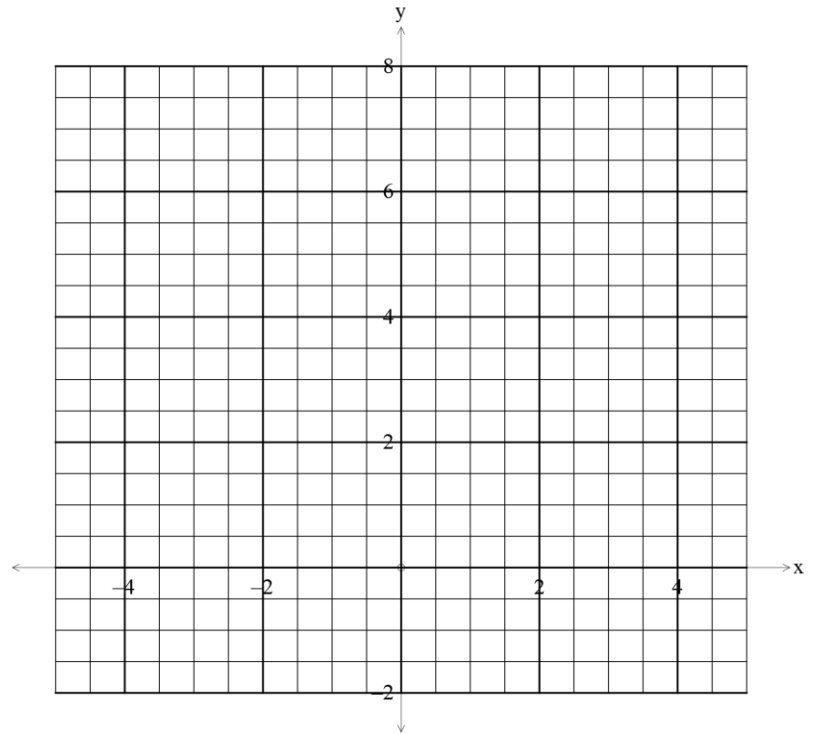
a.  $f(x) = 2|x - 3|$



b.  $g(x) = -|x + 1| + 2$



c.  $h(x) = |x + 1| + |x - 3|$



2. Solve the following equations involving absolute value functions, where the variable lies on the real number line.

a.  $|a + 1| = 5$

b.  $|2b - 5| = 13$

c.  $|-3c - 12| = -6$

d.  $|2d + 1| = |2d - 5|$

e.  $|2e + 1| = |e - 4|$

3. Solve the following equations involving absolute value functions, where the variable lies on the real number line.

a.  $|2a + 1| = |-a - 3|$

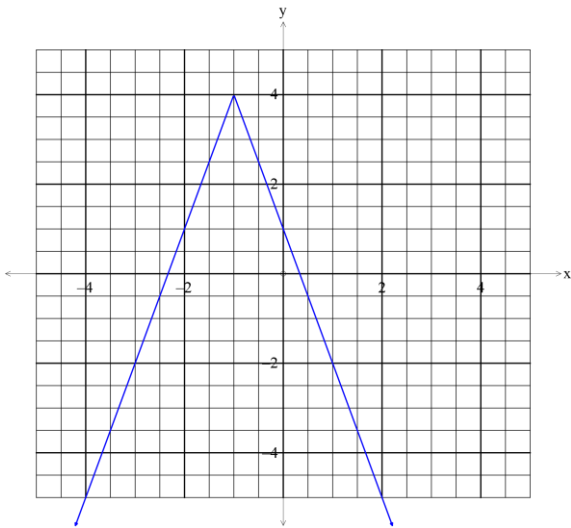
b.  $|b + 2| + |b - 2| = 6$

c.  $|c + 4| - |c - 1| = 1$

d.  $|d - 3| = |d + 2| + 3$

e.  $|e + 2| - 2 = |e - 1|$

4. The function presented is of the form  $y = a|bx + c| + d$ . Determine the values of  $a$ ,  $b$ ,  $c$  and  $d$ .



5. For each of the following problems, use a simple diagram to communicate your working.

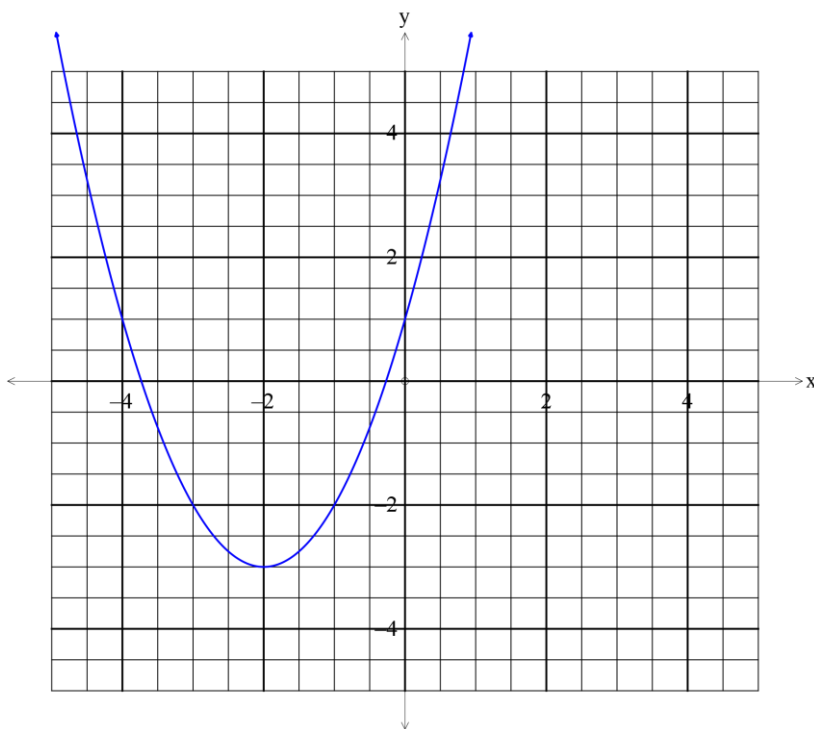
- a. Consider the inequality  $|x - a| \leq 6$ . If the solution set to this inequality is given by  $-2 \leq x \leq 10$ , determine the value of  $a$ .

- b. Consider the inequality  $-|2x - 3| + b \geq -3$ . If the solution set to this inequality is given by  $-\frac{1}{2} \leq x \leq \frac{7}{2}$ , determine the value of  $b$ .

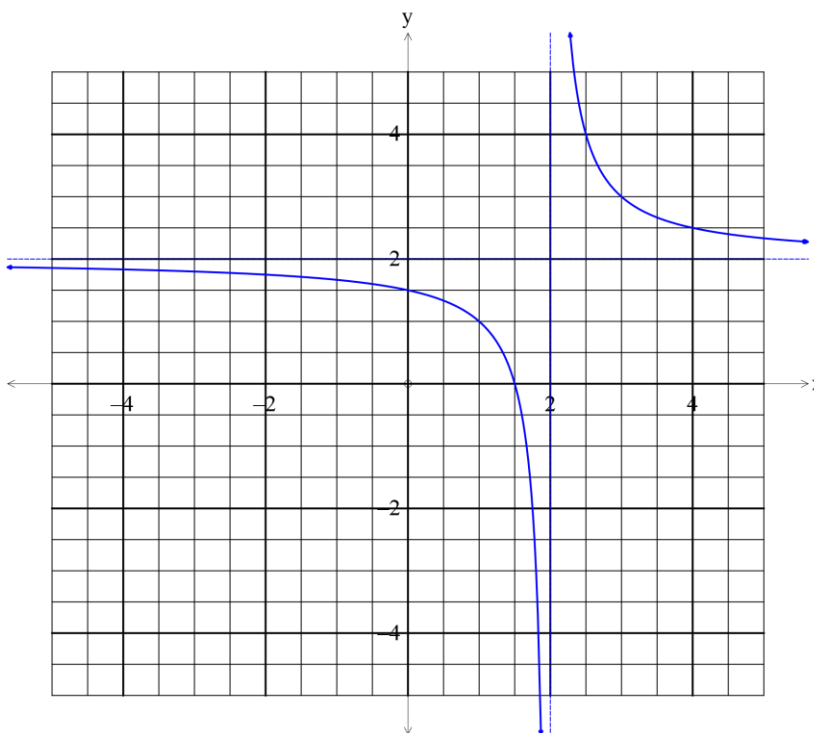
- c. Consider the equation  $|x + 2| = |x - c| - 3$ . If the solution set to this equation is given by  $x \leq -2$ , determine the value of  $c$ .

6. For each of the graphs  $f(x)$  presented, sketch  $\frac{1}{f(x)}$  on the same set of axes.

a.

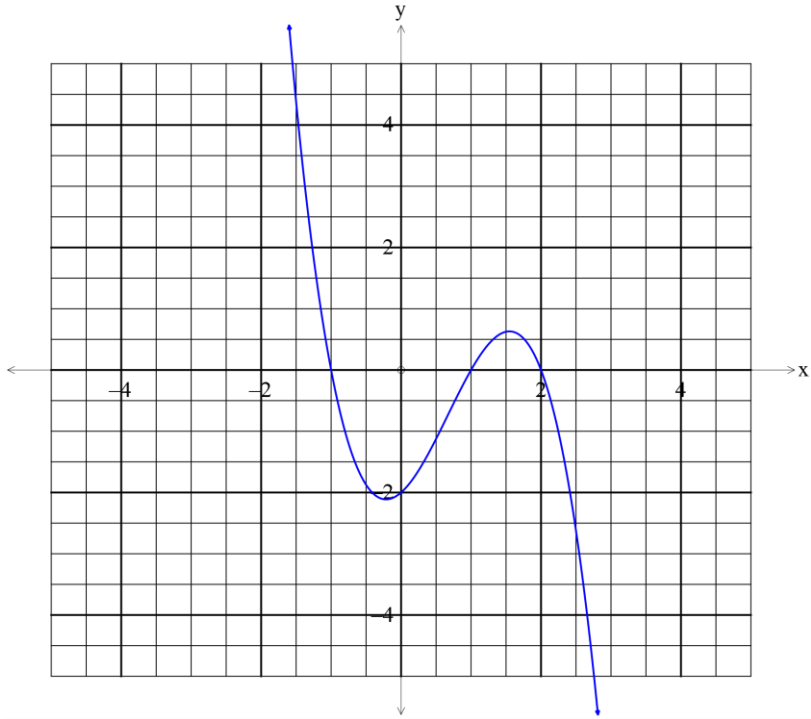


b.

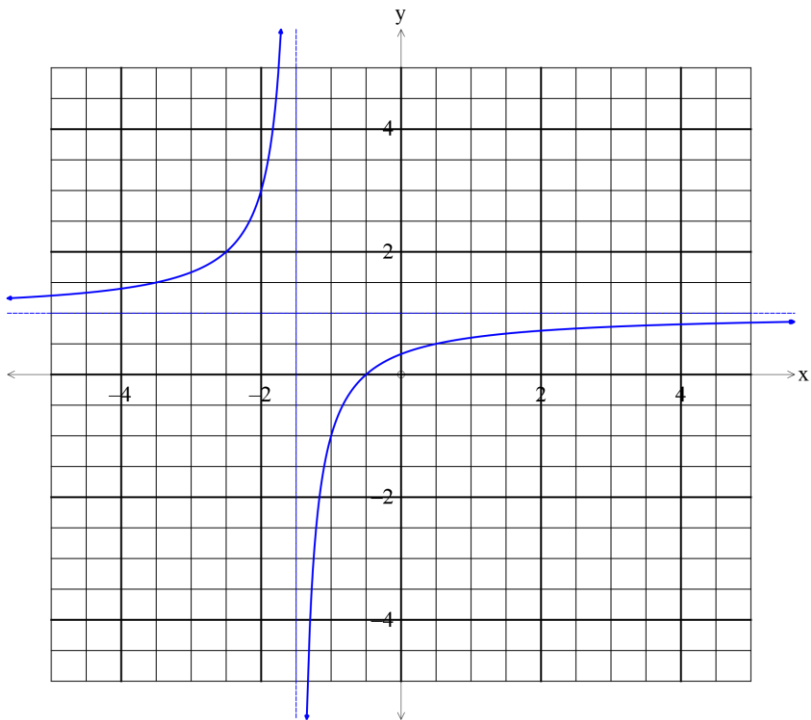


7. For each of the graphs  $f(x)$  presented, sketch  $|f(x)|$  on the same set of axes.

a.

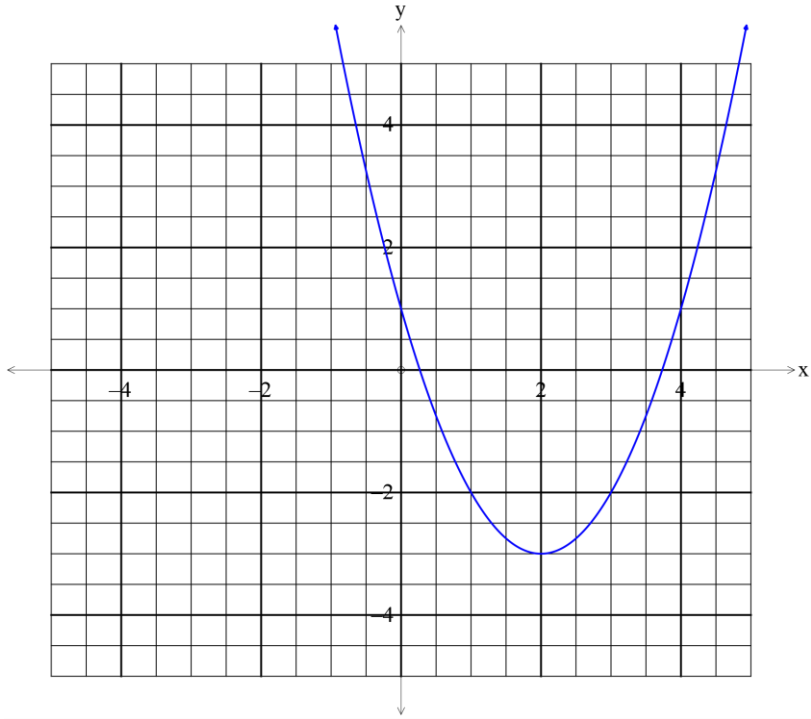


b.

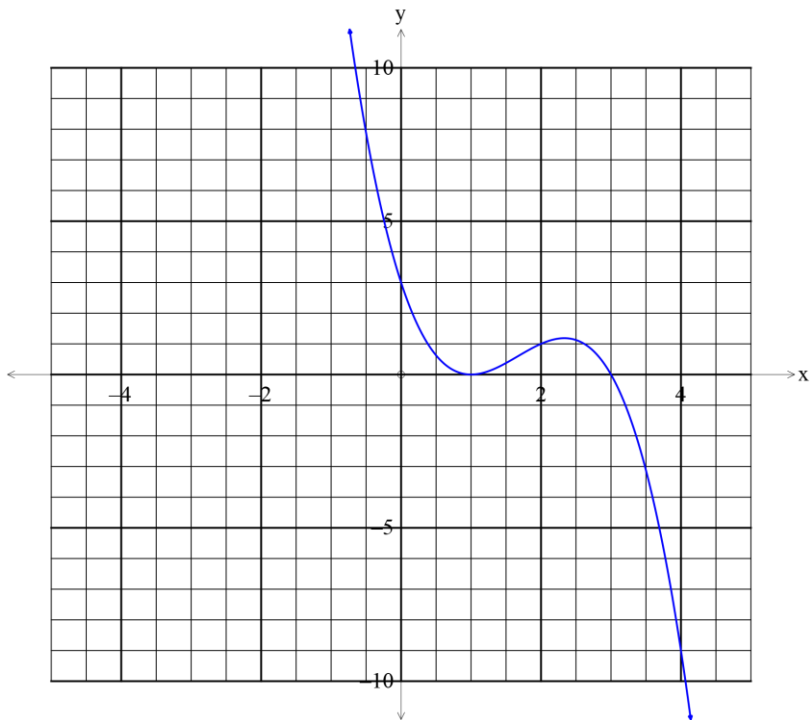


8. For each of the graphs  $f(x)$  presented, sketch  $f(|x|)$  on the same set of axes.

a.



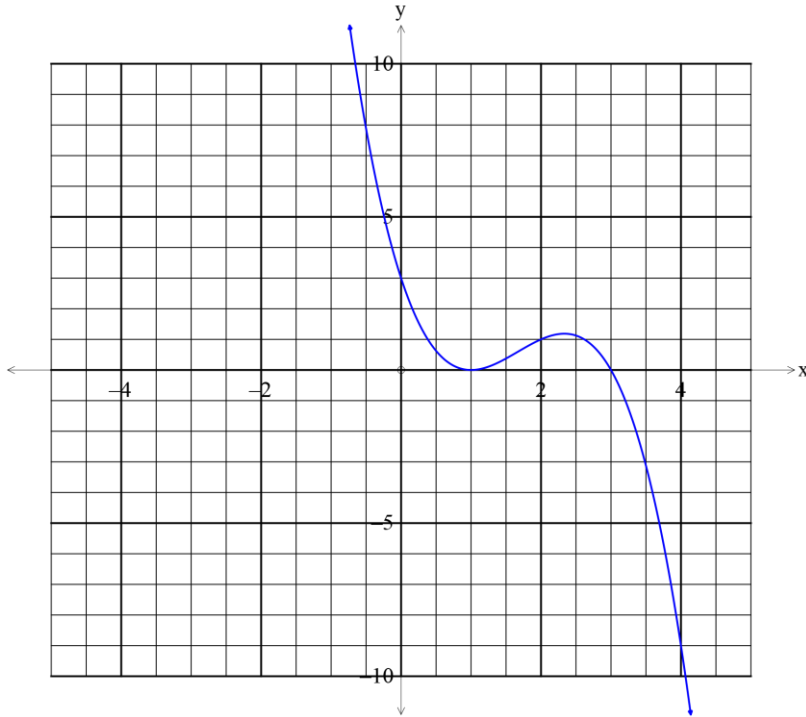
b.



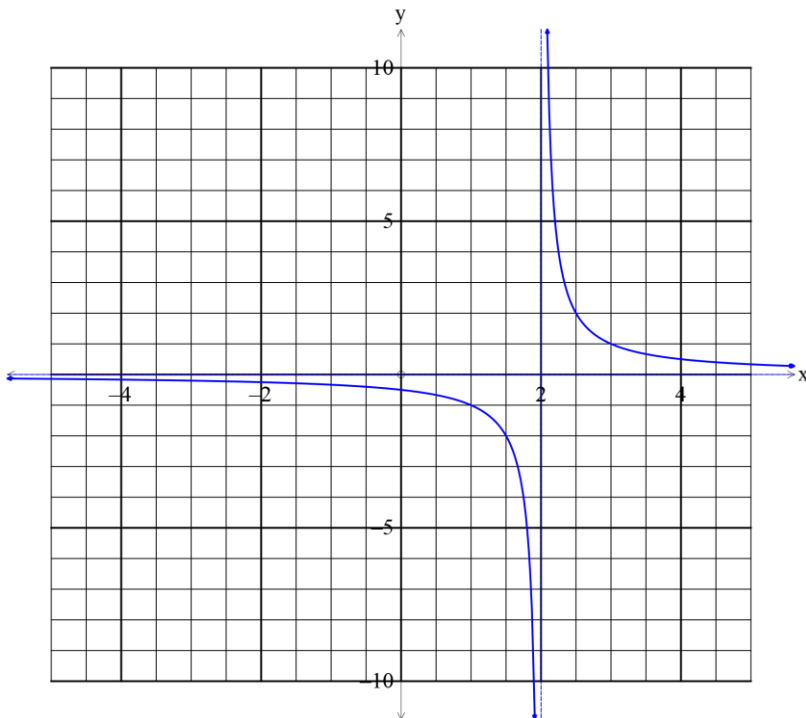


9. For each of the graphs  $f(x)$  presented, sketch  $|f(|x|)|$  on the same set of axes.

a.

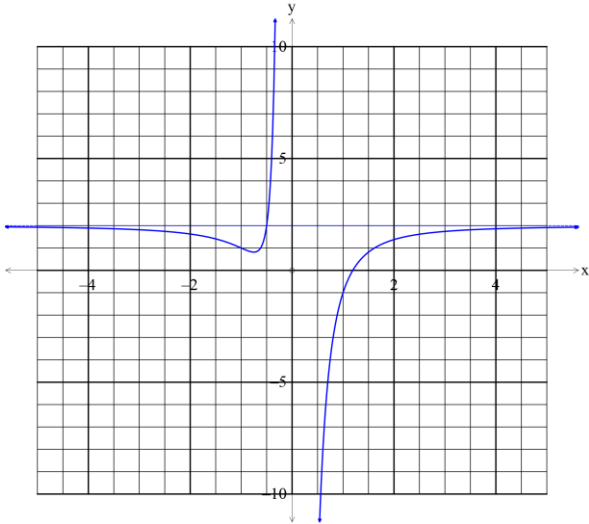


b.

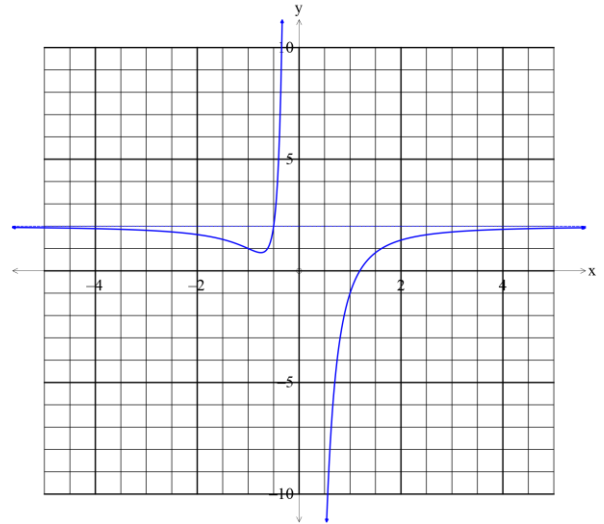


10. Some arbitrary  $f(x)$  is sketched on each set of axes. Upon each, complete the required sketch.

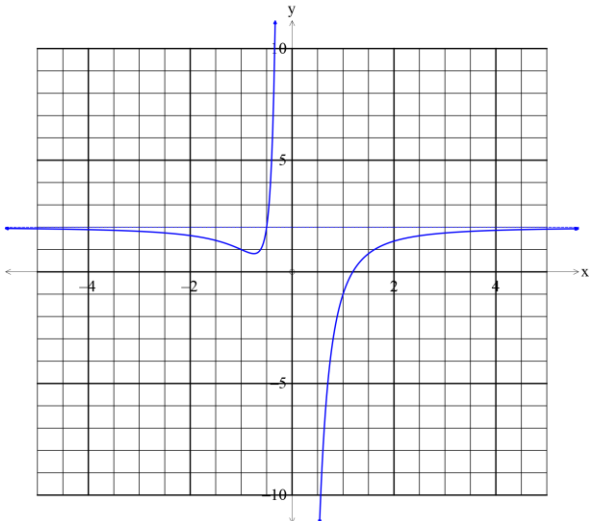
a.  $\frac{1}{f(x)}$



b.  $|f(x)|$



c.  $f(|x|)$



d.  $|f(|x|)|$

